## Cambridge Assessment International Education

Cambridge International General Certificate of Secondary Education

## MATHEMATICS (US)

0444/31
Paper 3 (Core)
May/June 2019
MARK SCHEME
Maximum Mark: 104

## Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.
Cambridge International is publishing the mark schemes for the May/June 2019 series for most Cambridge IGCSE ${ }^{\text {TM }}$, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

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## Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

## GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always whole marks (not half marks, or other fractions).

## GENERIC MARKING PRINCIPLE 3:

Marks must be awarded positively:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

## Abbreviations

| cao | correct answer only |
| :--- | :--- |
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| nfww | not from wrong working |
| soi | seen or implied |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 1(a) | $\frac{11}{15}$ [0].749 $\frac{3}{4} 76[\%]$ | 2 | B1 for 3 in the correct order or $0.75,(0.749), 0.76,0.73$. or $75 \%, 74.9 \%,(76 \%), 73 \ldots \%$ |
| 1(b) | 2 | 1 |  |
| 1(c) | 1236918 | 2 | B1 for 4 or 5 correct factors only or 6 correct factors with one extra or $1 \times 18,2 \times 9,3 \times 6$ |
| 1(d) | 4 or 8 | 1 |  |
| 1(e) | $\frac{1}{5}$ cao | 1 |  |
| 1(f) | 352 | 2 | M1 for $160 \div 5[\times 11]$ |
| 2(a) | 6.8[0] | 1 |  |
| 2(b) | $4.9[0]$ | 2 | M1 for $3.4[0]+2 \times[0] .85$ soi |
| 2(c)(i) | 280.5[0] | 1 |  |
| 2(c)(ii) | 379.5[0] | 2 | FT their $(\mathbf{c})(\mathbf{i})+99$ <br> M1 for $8 \times 1.5 \times 8.25$ soi <br> or $(8 \times 1.5+34) \times 8.25$ soi |
| 2(d) | 33 | 2 | M1 for 7.5, 7, 8, 10.5 |
| 2(e) | 85.20 cao | 3 | B2 for 85.1999... <br> OR <br> M1 for $9395 \div 110.27$ <br> B1 for their answer to at least 3 dp correctly rounded to 2 dp |
| 2(f) | $13891.5[0]$ | 3 | M2 for $12000 \times\left(1+\frac{5}{100}\right)^{3}$ oe or M1 for $12000 \times\left(1+\frac{5}{100}\right)^{2}$ oe |
| 3(a)(i) | Correct bar | 3 | M1 for 5, 12, 17 or 34 M1 for 40 - their 34 |
| 3(a)(ii) | 5 | 1 |  |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 3(a)(iii) | $\frac{12}{40}$ oe | 1 |  |
| 3(b)(i) | 86 | 1 |  |
| 3(b)(ii) | 45 | 2 | M1 for 18, 27, 31, 45, or 45, 60, 72, 104 |
| 3(b)(iii) | 51 | 2 | M1 for $\begin{aligned} & (104+18+72+31+27+45+60) \div 7 \\ & \text { soi } \frac{357}{7} \end{aligned}$ |
| 3(c) | Correct dot plot | 1 |  |
| 3(d) | Valid explanation e.g. Data which can take on any value oe | 1 |  |
| 4(a) | 56 | 2 | M1 for 180-118 soi by 62 |
| 4(b) | 144 | 3 | M2 for $180-(360 \div 10)$ oe M1 for $360 \div 10$ soi by 36 |
| 4(c) | $\begin{aligned} & 32 \\ & 58 \end{aligned}$ | 2 | B1 for each or for their $x+$ their $y=90$ or angle $F$ marked as 90 |
| 4(d) | 28 alternate | 2 | B1 for each |
| 4(e)(i) | 35 | 2 | M1 for $21^{2}+28^{2}$ or better |
| 4(e)(ii) | 31.9 or 31.92 to 31.93 | 3 | M2 for $[S U=] \frac{30}{\cos 20}$ or M1 for $\cos 20=\frac{30}{S U}$ oe |
| 5(a)(i) | $18 a$ final answer | 2 | M1 for $2 \times(7 a+2 a)$ oe |
| 5(a)(ii) | $14 a^{2}$ final answer | 2 | M1 for $7 a \times 2 a$ |
| 5(b) | 6914 | 2 | B1 for 2 correct or 569 |
| 5(c)(i) | -4-6-12 643 | 3 | B2 for 4 or 5 correct or B1 for 2 or 3 correct |
| 5(c)(ii) | Correct curve | 4 | B3FT for 9 or 10 points correctly plotted or B2FT for 7 or 8 points correctly plotted or B1FT for 5 or 6 points correctly plotted |
| 5(c)(iii) | Correct ruled line drawn | 1 |  |
| 5(c)(iv) | 1.3 to 1.7 | 1 | FT their curve and their line |
| 6(a) | 4 points correctly plotted | 2 | B1 for 2 or 3 points correctly plotted |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 6(b) | Positive | 1 |  |
| 6(c) | $(40,20)$ indicated | 1 |  |
| 6(d) | Ruled line of best fit | 1 |  |
| 6(e) | 33 to 42 | 1 | FT their positive line |
| 7(a) | Rotation [centre] ( 0,0 ) oe $90\left[^{\circ}\right]$ clockwise oe | 3 | B1 for each |
| 7(b) | Enlargement <br> [centre] (5, -7) <br> [sf=] 3 | 3 | B1 for each |
| 7(c) | Correct shape plotted with points $(6,-1)(8,-1)(6,-3)(8,-3)(6,-5)$ | 2 | B1 for a correct translation of $\binom{3}{k}$ or $\binom{k}{1}$ |
| 7(d) | Correct shape plotted with points $(-2,5)(-6,5)(-2,7)(-4,5)(-4,7)$ | 2 | B1 for reflection in $y=k$ or $x=1$ |
| 8(a) | $\pi \times 6^{2} \times 17$ | M1 |  |
|  | 1922.6 to 1922.91 | A1 |  |
| 8(b) | 36.5 or 36.53 to $36.54 \ldots$ | 5 | B2 for 100.53 to $100.54 \ldots$ or $32 \pi$ or M1 for $[0.5 \times] \pi \times 8^{2}$ oe and B2 for 64 or M1 for $[0.5 \times] 16 \times 8$ oe |
| 9(a) | $6 a+4 b$ final answer | 2 | B1 for $6 a+k b$ or $k a+4 b$ |
| 9(b) | 30 | 2 | M1 for $4 \times 3^{2}+3 \times-2$ or better |
| 9(c)(i) | 80 | 1 |  |
| 9(c)(ii) | 7 | 2 | M1 for $3 x=16+5$ or $x-\frac{5}{3}=\frac{16}{3}$ or better |
| 9(c)(iii) | 2.2 oe | 3 | M1 for $10 x+5$ [ $=27$ ] or $2 x+1=\frac{27}{5}$ <br> M1 for second correct step |
| 9(d) | $\frac{p+5}{3}$ or $\frac{p}{3}+\frac{5}{3}$ final answer | 2 | M1 for $p+5=3 r$ oe or $\frac{p}{3}=r-\frac{5}{3}$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :--- | ---: | :--- |
| $10($ a) | Correct ruled perpendicular bisector <br> with appropriate arcs <br> and <br> correct ruled angle bisector with <br> appropriate arcs <br> and lines intersecting | $\mathbf{4}$ | B2 for correct ruled perpendicular <br> bisector with appropriate arcs <br> or B1 for correct perpendicular bisector <br> drawn with no/ incorrect arcs or two pairs <br> of correct arcs with no line drawn |
| $10(b)$ | $110^{\circ}$ | B2 for correct ruled angle bisector with <br> appropriate arcs <br> or B1 for correct angle bisector drawn <br> with no/incorrect arcs or two pairs of <br> correct arcs with no line drawn |  |
| If lines do not intersect/meet, maximum 3 |  |  |  |
| marks |  |  |  |$|$| FT their $X$ |
| :---: |

